

Statistics

Lecture 11



Feb 19-8:47 AM

Class QZ 7

1) Complete the Venn Diagram below

$1 - .9 = .1$

A only

B only

1) $P(A) = \boxed{.4}$ ✓

2) $P(A \text{ and } B) = \boxed{.1}$

Total = 1

3) $P(A|B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.1}{.5} = \frac{1}{5} = \boxed{.2}$ ✓

Given

$P(B|A) = \frac{P(A \text{ and } B)}{P(A)} = \frac{.1}{.4} = \frac{1}{4} = \boxed{.25}$

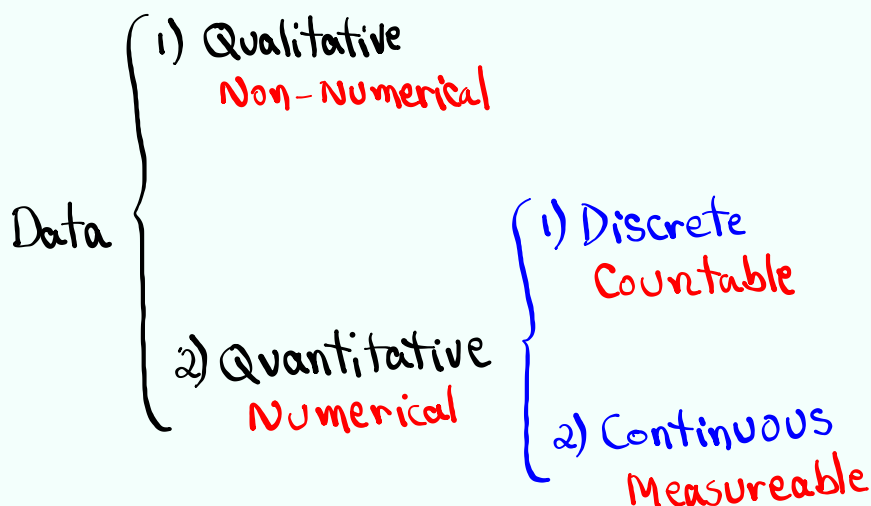
$P(A \text{ only or } B \text{ only}) = .3 + .4 = \boxed{.7}$

$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$

$= .4 + .5 - .1 = \boxed{.8}$

Apr 1-3:58 PM

SG 14



Apr 13-1:55 PM

Let x be a discrete random variable with
prob. dist. $p(x)$,

what is Prob. dist.? It is a method
to provide the prob. of all possible
outcomes.

- It could be in the form of
a table or chart.
- It could be in the form of
a graph.
- It could be in the form of
a formula.
- Just use the concept of Prob.

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Some rules:

$$1) 0 \leq P(x) \leq 1$$

$$2) \sum P(x) = 1$$

$$3) P(x) = 0 \leftrightarrow \text{Impossible event}$$

$$4) P(x) = 1 \leftrightarrow \text{Sure event}$$

$$5) 0 < P(x) \leq .05 \leftrightarrow \text{Rare event}$$

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Consider the chart below

x	$P(x)$
1	.2
2	.5
3	.3

$$1) \text{ verify } \sum P(x) = 1$$

$$.2 + .5 + .3 = 1 \checkmark$$

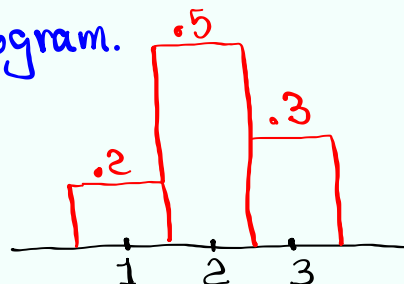
$$2) P(x \geq 2) = .5 + .3 = \boxed{.8}$$

$$3) P(x \leq 2) = .5 + .2 = \boxed{.7}$$

4) Draw Prob. dist. histogram.

$x \rightarrow$ midpt

$P(x) \rightarrow$ Rel. F.



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Consider the chart below

x	P(x)
1	.1
2	.2
3	.5
4	?.2

1) $P(x=4)$
 $= 1 - (.1 + .2 + .5) = 1 - .8 = .2$
 Total Prob.

2) $P(x=2 \text{ or } x=3)$
 $.2 + .5 = .7$

3) $P(x \geq 2)$
 $= .2 + .5 + .2 = .9$
 $\rightarrow = 1 - P(x=1) = 1 - .1 = .9$

4) Draw Prob. dist. histogram

$x \rightarrow$ MP
 $P(x) \rightarrow$ Rel. F.

Apr 13-2:13 PM

Complete the chart below

x	P(x)	xP(x)	x ² P(x)
2	.2	.4	.8
3	.5	1.5	4.5
4	.3	1.2	4.8

1) $\sum P(x) = 1 \checkmark$

2) $\sum xP(x) = 3.1 \checkmark$

3) $\sum x^2 P(x) = 10.1 \checkmark$

4) Compute $\sum x^2 P(x) - (\sum xP(x))^2$
 $= 10.1 - 3.1^2 = .49$

5) Find $\sqrt{\text{Last Answer}} = \sqrt{.49} = .7$

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Complete the chart below

x	$P(x)$	$xP(x)$	$x^2P(x)$
1	.2	.2	.2
2	.3	.6	1.2
3	.3	.9	2.7
4	.2	.8	3.2

1) $P(X=1)$
 $= 1 - [.3 + .3 + .2]$
 $= .2$

2) $P(X=1 \text{ or } X=4)$
 $= .2 + .2 = .4$

3) $\sum xP(x) = 2.5$

4) $\sum x^2P(x) = 7.3$

5) Compute $\sum x^2P(x) - (\sum xP(x))^2$
 $= 7.3 - 2.5^2 = 1.05$

6) $\sqrt{\text{last answer}} = \sqrt{1.05} \approx 1.025 \approx 1$

7) Draw Prob. dist. Histogram.

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Mean μ (mu) $\mu = \sum xP(x)$

Variance σ^2 (Sigma²) $\sigma^2 = \sum x^2P(x) - \mu^2$

Standard deviation σ (Sigma) $\sigma = \sqrt{\sigma^2}$

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x	$P(x)$	$xP(x)$	$x^2P(x)$
2	.3	.6	1.2
3	.5	1.5	4.5
4	.2	.8	3.2

$\mu = \sum xP(x) = .6 + 1.5 + .8 = \boxed{2.9}$
 $\sigma^2 = \sum x^2P(x) - \mu^2 = 1.2 + 4.5 + 3.2 - 2.9^2 = \boxed{.49}$
 $\sigma = \sqrt{\sigma^2} = \sqrt{.49} = \boxed{.7}$

now using TI List: L1, Freq List: L2
 clear all lists
 $x \rightarrow L1, P(x) \rightarrow L2$
STAT **CALC**
1-Var Stats

$\mu = \bar{x} = \boxed{2.9}$ **VARs**
 $\sigma = \sigma_x = \boxed{.7}$ **5: Statistics**
 $n = 1 \checkmark$ **4: σ_x** **x^2**
 $\sigma^2 = \sigma_x^2 = \boxed{.49}$ **Enter**

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A piggy bank has 2 nickels and 8 dimes.
 Select 2 coins with replacement.

Sample space Tree diagram

$NN \rightarrow 10\text{¢} \quad P(10\text{¢}) = \frac{2}{10} \cdot \frac{2}{10} = \frac{4}{100} = \boxed{.04}$
 $ND \rightarrow 15\text{¢} \quad P(15\text{¢}) = 2 \cdot \frac{2}{10} \cdot \frac{8}{10} = \frac{32}{100} = \boxed{.32}$
 $DN \rightarrow 15\text{¢} \quad P(15\text{¢}) = \frac{8}{10} \cdot \frac{2}{10} = \frac{16}{100} = \boxed{.16}$
 $DD \rightarrow 20\text{¢} \quad P(20\text{¢}) = \frac{8}{10} \cdot \frac{8}{10} = \frac{64}{100} = \boxed{.64}$

Total	$P(\text{Total})$
10¢	.04
15¢	.32
20¢	.64

$\mu = \bar{x} = 18$ **VARs**
 $\sigma = \sigma_x = 2.828$ **5: Statistics**
 $n = 1 \checkmark$ **4: σ_x** **x^2**
Enter
 $\sigma^2 = 8$

Total $\rightarrow x \rightarrow L1$
 $P(\text{Total}) \rightarrow P(x) \rightarrow L2$
 use **1-Var Stats**
 with $L1 \neq L2$

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$\mu = 18$ $\sigma \approx 3$
 68% Range $\rightarrow \mu \pm \sigma = 18 \pm 3 \rightarrow \boxed{15 \text{ to } 21}$
 95% Range $\rightarrow \mu \pm 2\sigma = 18 \pm 2(3) \rightarrow \boxed{12 \text{ to } 24}$
 Usual Range
 99.7% Range $\rightarrow \mu \pm 3\sigma = 18 \pm 3(3) \rightarrow \boxed{9 \text{ to } 27}$

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2 Females, 3 Males, Select 2 people
 No replacement

Sample space

$P(2 \text{ Females}) = P(FF) = \frac{2}{5} \cdot \frac{1}{4} = \frac{2}{20} = \frac{1}{10} = \boxed{.1}$
 $P(1 \text{ Female}) = P(FM \text{ or } MF) = 2 \cdot \frac{2}{5} \cdot \frac{3}{4} = \frac{12}{20} = \boxed{.6}$
 $P(0 \text{ Female}) = P(MM) = \frac{3}{5} \cdot \frac{2}{4} = \frac{6}{20} = \boxed{.3}$

# F	P(#F)
2	.1
1	.6
0	.3

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#F → L1
P(#F) → L2

L1	L2
2	.1
1	.6
0	.3

Use **1-Var Stats**
with L1 & L2
List: L1
FreqList: L2

VAR S
5: Statistics
4: σ_x χ^2
Math 1: ▸ Frac **Enter**

$\sigma^2 = \frac{9}{25}$
 $\mu = \bar{x} = .8$
 $\sigma = \sigma_x = .6$
 $n = 1 \checkmark$

Apr 13-3:23 PM

Expected Value:

I sold 20 TKTS for \$10 each.
one TKT randomly drawn, winner gets a
Calculator worth \$120.

expected value **per TKT** Sold.

Method I:
20 TKTS × \$10 each = \$200
\$200 - \$120 = \$80 Net Profit
\$80 ÷ 20 TKts = **\$4/TKT**

Method II:

Net	P(Net)
10-120	1/20 House loses
10-0	19/20 House wins

net → L1
P(Net) → L2
1-Var Stats
with L1 & L2
E.V. = $M = \bar{x}$
 $\mu = \$4$

$\sigma^2 = 684$

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You pay \$100 to buy insurance for your luggage.

Any accident \rightarrow Policy pays \$1000

Prob. of any accident is $\boxed{.2\%} \rightarrow .002$

Find expected Value per policy Sold.

Net	P(Net)	
100 - 1000	.002	Damage
100 - 0	.998	Damage

$$\sigma^2 = 1996$$

Net \rightarrow L1

P(Net) \rightarrow L2

1-var Stats

with L1 & L2

$$E.V. = \mu = \bar{x}$$

$$\boxed{\$ 98}$$

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Pay me \$10 and draw one card from a standard deck of playing cards.

If you draw Ace \rightarrow I give you \$50

If you " Face \rightarrow I give you \$10

Any other card \rightarrow I give you nothing.

net	P(Net)	
10 - 50	4/52	Ace
10 - 10	12/52	Face
10 - 0	36/52	any other card

$$\sigma^2 = \frac{30000}{169}$$

net \rightarrow L1

P(Net) \rightarrow L2

1-var Stats

with L1 & L2

$$E.V. = \mu = \bar{x}$$

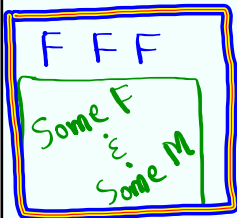
$$\approx \$3.85$$

$$\boxed{\$ 14 \& 15} \checkmark$$

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12 Students

8 Females, 4 Males, Select 3 Students



$$P(\text{all Females}) = \frac{8}{12} \cdot \frac{7}{11} \cdot \frac{6}{10} = \boxed{\frac{14}{55}}$$

$$P(\text{all Males}) = \frac{4}{12} \cdot \frac{3}{11} \cdot \frac{2}{10} = \boxed{\frac{1}{55}}$$

$$P(\text{at least 1 Female}) = 1 - P(\text{No Female})$$

$$= 1 - P(\text{All males})$$

$$= 1 - \frac{1}{55} = \boxed{\frac{54}{55}}$$

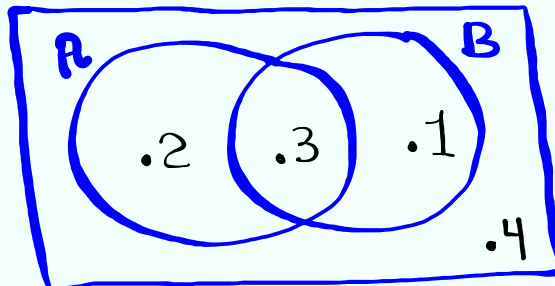
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$$P(A) = .5$$

$$P(B) = .4$$

$$P(A \text{ and } B) = .3$$

1) Make Venn Diagram



$$2) P(B|A)$$

$$= \frac{P(A \text{ and } B)}{P(A)} = \frac{.3}{.5} = \boxed{.6}$$

Apr 13-4:00 PM

$$P(A) = .6$$

$$P(B) = .5$$

$$P(A|B) = .8$$

Find $P(A \text{ and } B)$

$$P(A|B) = \frac{P(A \text{ and } B)}{P(B)}$$

$$.8 = \frac{P(A \text{ and } B)}{.5}$$

Cross-Multiply

$$P(A \text{ and } B) = (.8)(.5) = \boxed{.4}$$

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